

Package: adlaplaceFem (via r-universe)

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Type Package

Title Finite Element Approximations for Adlaplace

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Description Finite-element approximations for hierarchical models with the adlaplace Laplace approximation framework. Currently provides tensor-product B-spline FEM ingredients for Matern Gaussian random fields (mass, stiffness, and higher-order Grams), design and Gram matrix construction on regular grids, optional terra SpatRaster / SpatVector input, and AD tape builders for random_fem_ssq_* / random_fem_det_*.

SystemRequirements OpenMP

License MPL-2.0

Depends R (>= 4.1.0), adlaplace (>= 0.5.3)

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LinkingTo Rcpp, adlaplace, RcppEigen, trustOptim, Matrix, RCppAD

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fem_bspline	<i>Tensor-product B-spline FEM ingredients for a 2D Matern GRF</i>
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Description

Builds the design matrix of tensor-product B-splines at evaluation coordinates together with sparse mass, stiffness, and higher-order Gram matrices used in the SPDE FEM precision for operator orders $\alpha = 2$ and 3 .

Usage

```
fem_bspline(coords, knots, degree = 2L, ...)  
  
## S4 method for signature 'list'  
fem_bspline(coords, knots, degree = 2L, ...)  
  
## S4 method for signature 'data.frame'  
fem_bspline(coords, knots, degree = 2L, ...)
```

Arguments

- `coords` Evaluation locations. For a `data.frame` (e.g. `sites_eval` from `expand.grid`), rows are point coordinates with columns `x` and `y`. For a plain `list(x, y)` of axis sequences, the full tensor grid is formed with `expand.grid`. With **terra**, `SpatRaster` / `SpatVector` are also accepted.
- `knots` Knot-line positions on each axis: `list(x = seq(...), y = seq(...))` of unique increasing breakpoints (domain endpoints included). These are expanded to open B-spline knot vectors. With **terra**, a `SpatRaster` whose grid defines knot lines is also accepted.

degree B-spline degree; must be ≥ 2 . Default 2 ($\alpha = 2$). Use degree = 3 when assembling G3 for $\alpha = 3$.

... Passed to methods (unused for list / data.frame).

Details

Coefficient ordering is column-major (vec) over the n_x by n_y array of tensor basis indices: basis (i, j) maps to column $i + (j - 1) * n_x$.

Value

A list with:

A dgCMatrix design, n by $n_x * n_y$

C, G, G2 sparse Grams

G3 sparse Gram or NULL if degree < 3

degree, knots, n_basis metadata ($n_basis = c(n_x, n_y)$)

Examples

```
sites_list <- list(x = seq(0, 1, by = 0.25), y = seq(0, 1, by = 0.25))
sites_eval <- do.call(expand.grid, sites_list)
fem <- fem_bspline(sites_eval, sites_list, degree = 2L)
```

fem_chol_pattern	<i>Symbolic LDL pattern for a sparse FEM precision structure</i>
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Description

Builds the permutation and unit-lower pattern required by adlaplace's chol_update for a precision with the same sparsity as Q_structure (typically the union of FEM Gram patterns).

Usage

```
fem_chol_pattern(Q_structure)
```

Arguments

Q_structure Symmetric sparse matrix with the structural nonzeros of $Q(\theta)$ (numeric values only need to make the matrix positive definite for symbolic analysis; diagonals are inflated if needed).

Value

A list with perm (0-based), L1 (dtCMatrix / unit lower), and perm_inv (0-based), suitable for the chol slot of a random_fem_* precision payload.

fem_precision	<i>Assemble FEM Matern precision Q2 or Q3 from Grams</i>
---------------	--

Description

Assemble FEM Matern precision Q2 or Q3 from Grams

Usage

```
fem_precision(kappa, tau, C, G, G2, G3 = NULL, alpha = 2L)
```

Arguments

kappa, tau	Positive SPDE parameters.
C, G, G2, G3	Sparse Grams from fem_bspline() .
alpha	2 or 3.

Value

Sparse dgCMatrix precision.

fem_precision_payload	<i>Build random_fem_ssq_* / random_fem_det_* precision payload for adlaplace</i>
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Description

Build random_fem_ssq_* / random_fem_det_* precision payload for adlaplace

Usage

```
fem_precision_payload(fem, alpha = 2L)
```

Arguments

fem	Result of fem_bspline() (or list with C, G, G2, optional G3).
alpha	2 or 3.

Value

List for ad_data@precision: Grams, chol pattern, and Q CSC coefficients aligned for on-tape assembly.

fem_Q_structure	<i>Structural nonzero pattern for Q2 or Q3 from Grams</i>
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Description

Structural nonzero pattern for Q2 or Q3 from Grams

Usage

```
fem_Q_structure(C, G, G2, G3 = NULL)
```

Arguments

C, G, G2, G3 Sparse Grams from [fem_bspline\(\)](#); G3 may be NULL for alpha = 2.

Value

Symmetric sparse matrix with the union of Gram nonzero patterns.

matern-class	<i>Matern FEM spatial random field term</i>
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Description

Formula term for a 2D Matern GRF via tensor-product B-spline FEM, wired to `adlaplaceFem` kernels `random_fem_ssqr_2 / random_fem_det_2` (shape `nu = 1`) or `random_fem_ssqr_3 / random_fem_det_3` (`nu = 2`). The quadratic form is a random shard; the log-determinant is a parameters companion via [adlaplace::extra_ad_fun\(\)](#). The first argument is a **column name** in data (like [adlaplace::iid\(\)](#)): that column holds observation locations as a 2-column matrix, WKT text, or HEX WKB points. Knot lines are supplied at construction; the observation design matrix is built later in [adlaplace::design\(\)](#) from data.

Usage

```
matern(
  x,
  knots,
  shape = 1L,
  init = c(1, 1),
  lower = c(1e-09, 1e-09),
  upper = c(Inf, Inf),
  parscale = c(1, 1)
)

## S4 method for signature 'matern'
extra_ad_fun(term)
```

```
## S4 method for signature 'matern'
design(term, data)

## S4 method for signature 'matern'
precision(term, data)

## S4 method for signature 'matern'
random_info(term, data)

## S4 method for signature 'matern'
theta_info(term)

## S4 method for signature 'matern'
beta_info(term, data)
```

Arguments

x	Name of the geometry / coordinate column in data.
knots	Knot lines as <code>list(x = ..., y = ...)</code> or a terra <code>SpatRaster</code> (extent endpoints plus interior cell centers).
shape	Matern smoothness nu (1 or 2). Default 1L (SPDE alpha = 2, quadratic B-splines). Use 2 for nu = 2 / cubic B-splines.
init	Initial values for (range, sd) on the natural scale, where range = $\sqrt{8 \cdot \text{nu}} / \text{kappa}$ is the practical range (same units as coordinates; matches geostatsp/INLA) and sd is the marginal SD of the Matern field. Internally converted to SPDE (kappa, tau).
lower, upper	Bounds for (range, sd).
parscale	Optimization scales for (range, sd).
term	A <code>matern</code> term.
data	Model data frame (passed by <code>adlaplace</code> generics).

Details

In 2D, B-spline degree and SPDE order alpha equal shape + 1.

Value

A `matern` term object.

Functions

- `extra_ad_fun(matern)`: Companion parameters density for the FEM log-determinant shard.
- `design(matern)`: Design matrix of B-spline basis evaluations at coordinates in `data[[term@term]]`.
- `precision(matern)`: FEM precision payload for `random_fem_*`.
- `random_info(matern)`: Random-effect metadata (one row per basis weight).

- `theta_info(matern)`: Theta info for practical range = $\sqrt{8 \cdot \nu} / \kappa$ and field sd (log scale when `transform_theta` is TRUE).
- `beta_info(matern)`: Beta info (none).

matern_est

Posterior mean, SD, and simulations of a matern field on a raster

Description

Evaluates the fitted Matern GRF on `eval_grid` under the Laplace approximation for the random effects (outer parameters fixed at the MLE). Returns a `SpatRaster` with layers mean, sd, and optionally `sim1 ... simn`.

Usage

```
matern_est(fit, eval_grid, n = 0L)
```

Arguments

<code>fit</code>	An "adlaplace_fit" from <code>adlaplace::adlaplace()</code> that includes exactly one <code>matern()</code> term.
<code>eval_grid</code>	A terra <code>SpatRaster</code> whose cell centers are evaluation sites.
<code>n</code>	Number of posterior simulations of the field. Default 0 (mean and sd only).

Value

A `SpatRaster` with `n + 2` layers: mean, sd, and `sim1...simn` when `n > 0`.

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